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## CLASSICAL SOLUTIONS FOR THE SEMI-LINEAR MOORE-GIBSON-THOMPSON EQUATION

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ABSTRACT. This paper is devoted to the Cauchy problem for the semi-linear Moore-Gibson-Thompson equation. The considered Cauchy problem is investigated for existence of at least one classical solution. In the paper is proposed a new topological approach for investigation for existence of classical solutions based upon a recent theoretical result.

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